An experimental and numerical approach to UT responses and their POD curves

M. Carboni
Fatigue is the **most** important source of failure for mechanical components during **service**

Particularly, initiation sites, in the **most** critical sections, can be observed in correspondence of production or service **defects** (also due to the environment)

The most appropriate **design** approach in this scenario is the **Damage Tolerance**: to determine the most opportune inspection interval given the **POD** curve of the adopted NDT method or vice versa
NDT performance is usually **quantified** and **summarised** using the POD curve which relates the probability to detect a defect with a characteristic **linear** dimension (length, depth, diameter, …)

**Railway axles**

Actually, a POD curve is also a function of many other factors:

- material
- time of flight
- geometry
- equipment
- operator (human factor)
- …

Consequently, it is **rarely** possible to apply the POD curve obtained for a given configuration to another one, even if **similar**
Introduction

Another critical aspect of POD curves is the need to statistically characterise the largest defect that can be missed and not the smallest that can be detected.

Consequently, POD curves should be always given together with a suitable confidence level (usually 95%) needing a high number of tests to be determined.

In the present research, the special case of the UT inspection of hollow railway axles made of A4T steel is considered in order to:

- describe a novel methodology for the interpretation of UT responses with the aim to generalise, at least for some aspects, the POD curve
- investigate the possibility to apply the Model-Assisted Probability of Detection (MAPOD) methodology where, with the aim to diminish the experimental effort, part of it is substituted by proper numerical simulations
“Reflecting Area” approach

- Gilardoni RDG500
- Probe: ATM 45/4, 8x9 mm
- Plexiglas wedge ($V_L = 2700 \text{ m/s}$ and $V_S = 1100 \text{ m/s}$)
- Coupling: grease
- Reference: 48 dB

- Hollow axles: $D_{\text{ext}} = 152 \text{ mm}$, $D_{\text{int}} = 65 \text{ mm}$
- A4T: $V_L = 5920 \text{ m/s}$ and $V_S = 3230 \text{ m/s}$

- Twenty artificial defects
- 1st leg and 2nd leg inspections
"Reflecting Area" approach

1st leg configuration

$\mu_{log_{10}(a)} = 0.96 + 0.931 \times \log_{10}(a)$

$R^2 = 0.75$

Response $\hat{a}$ [%]

Notch depth $a$ [mm]

2nd leg configuration

$\mu_{log_{10}(a)} = 0.29 + 0.886 \times \log_{10}(a)$

$R^2 = 0.64$

Response $\hat{a}$ [%]

Notch depth $a$ [mm]

$\sigma_{log_{10}(a)} = 0.26$

$\sigma_{log_{10}(a)} = 0.34$
“Reflecting Area” approach

Crack or notch \( A_{\text{crack}} \)

Sound beam \( A_{\text{beam}} \)

\[
\hat{\Lambda} = A_{\text{crack}} / A_{\text{beam}}
\]

Graph showing relationship between reflecting area and response percentage.

Mathematical equation:

\[
\mu_{\log_{10}(A)} = 0.41 + 0.809 \log_{10}(A)
\]

\( R^2 = 0.97 \)

\[
\mu_{\log_{10}(A)} = 0.32 + 0.797 \log_{10}(A)
\]

\( R^2 = 0.98 \)
“Reflecting Area” approach
"Reflecting Area" approach

- Reflecting area vs. crack depth
- Reflecting area vs. notch or crack depth
- Reflecting area vs. reflecting area

Mathematical equations and statistical parameters are provided for each graph.
It is possible to conclude that:

- depth is not the best parameter to characterise UT response, the area actually invested by the sound beam seems to give better results
- defects characterised by different shapes, but the same depth, can have completely different POD curves
- adopting the proposed approach, POD curves assume a more general applicability because independent from the defect shape

There are some open points: angle between the sound beam and the defect, reflection on a curve surface

Unfortunately, the results shown so far, required an expensive amount of time and costs

So, why do not try a MAPOD approach?
POD curves are based on the statistical distribution of UT responses which, on the other hand, are controlled by numerous factors related to the adopted NDT procedure.

Today, many of such factors can be modelled and simulated by suitable physical and numerical models and MAPOD uses this possibility at its best. Unfortunately, MAPOD does not allow to completely avoid experimental tests because not all of such factors can be, at the moment, described by known physical models.

Two different versions of MAPOD exist today.

Transfer function

Complete approach
Both the two versions can be successfully applied to the case of railway axles

In this research, the numerical tools used for simulations is CIVA 10.0b. Its calibration was carried out simulating the 2\textsuperscript{nd} leg UT response of the 8 mm convex artificial defect and imposing to such response to be equal to the experimental one. Eventually, keeping the same gain, other defects with different reflecting areas were simulated.
The calibrated numerical model was then used to predict 1\textsuperscript{st} leg UT response of defects

In this way:

- it was possible to consider a situation similar to the calibration, but with a significantly different parameter (time of flight)
- experimental responses in 1\textsuperscript{st} leg configuration are available in order to validate the simulations
The just presented results represent a good first level of simulation that could be useful in some scenarios, but they are not able to provide info about the experimental intrinsic variability. The confidence band of numerical results is fictitious and not representative of experiments. It is then necessary to adopt the MAPOD complete approach which requires to adopt, during simulations and for each variability source, a suitable statistical distribution from which to extract values following a Monte Carlo methodology.

For simplicity, just one variability source was here considered: the longitudinal position of the probe. A Gaussian was adopted characterised by a mean equal to the position maximising the echo and CV=0.1.

For each simulated defect, 30 runs were carried out (total 150).
The best responses coincide with the calibration because this was deterministically carried out at the position of the maximised echo. The others are lower because not optimised.

The standard deviation obtained with this methodology seems to be significant.
Derivation of POD curves

\[
\begin{align*}
\mu_{\log_{10}(\hat{A})} & = \beta_0 + \beta_1 \cdot \log_{10}(A) \\
\sigma_{\log_{10}(\hat{A})} & = \beta_2
\end{align*}
\]

\[
POD(A) = Pr \left[ \log_{10}(\hat{A}) > \log_{10}(\hat{A}_{th}) \right]
\]

\[
POD(A) = 1 - F \left\{ \frac{\log_{10}(\hat{A}_{th}) - [\beta_0 + \beta_1 \cdot \log_{10}(A)]}{\beta_2} \right\} =
\]

\[
F \left\{ \frac{\log_{10}(A) - \left[ \frac{\log_{10}(\hat{A}_{th}) - \beta_0}{\beta_1} \right]}{\frac{\beta_2}{\beta_1}} \right\}
\]

\[
\mu = \frac{\log_{10}(\hat{a}_{th}) - \beta_0}{\beta_1} \quad \sigma = \frac{\beta_2}{\beta_1}
\]
The decision threshold was here chosen as the saw-cut with depth equal to 1 mm.

**Calibration**

**Transfer function**
Derivation of POD curves

Complete approach

![Graph showing POD curves and reflecting area](image)
Conclusions

In the present research, considering the special case of hollow railway axles made of A4T steel, some improvements of the procedure for deriving the UT POD curves were analysed. The obtained results can be so summarised:

• the “reflecting area” approach allows to generalise, at least in terms of defect morphology, the application of POD curves

• the results obtained from both the MAPOD versions seem to be encouraging because good predictions of experimental results could be achieved

• there is effectively a possibility to diminish the experimental effort maintaining the same reliability of the inspection

• the MAPOD approach is very recent (2003), so much work must still be done

• we are also starting to analyse the noise distribution in order to include the influence of PFA